A mathematical model of compartmentalized neurotransmitter metabolism in the human brain

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Gruetter, Rolf, Elizabeth R. Seaquist, and Kâmil Ugurbil. A mathematical model of compartmentalized neurotransmitter metabolism in the human brain. Am J Physiol Endocrinol Metab 281: E100–E112, 2001.—After administration of enriched [1,13C]glucose, the rate of 13C label incorporation into glutamate C4, C3, and C2, glutamine C4, C3, and C2, and aspartate C2 and C3 was simultaneously measured in six normal subjects by 13C NMR at 4 Tesla in 45-ml volumes encompassing the visual cortex. The resulting eight time courses were simultaneously fitted to a mathematical model. The rate of (neuronal) tricarboxylic acid cycle flux (Vsyn) 0.57 ± 0.06 μmol·g−1·min−1, was comparable to the exchange rate between (mitochondrial) 2-oxoglutarate and (cytosolic) glutamate (Vcyt 0.57 ± 0.19 μmol·g−1·min−1), which may reflect to a large extent malate-aspartate shuttle activity. At rest, oxidative glucose consumption [CMRGlc(ox)] was 0.41 ± 0.03 μmol·g−1·min−1, and (glial) pyruvate carboxylation (VPC) was 0.09 ± 0.02 μmol·g−1·min−1. The flux through glutamine synthetase (Vsyn) was 0.26 ± 0.06 μmol·g−1·min−1. A fraction of Vsyn was attributed to be from (neuronal) glutamate, and the corresponding rate of apparent glutamatergic neurotransmission (VNT) was 0.17 ± 0.05 μmol·g−1·min−1. The ratio [VNT/CMRGlc(ox)] was 0.41 ± 0.14 and thus clearly different from a 1:1 stoichiometry, consistent with a significant fraction (∼90%) of ATP generated in astrocytes being oxidative. The study underlines the importance of assumptions made in modeling 13C labeling data in brain.

nuclear magnetic resonance; glutamate; neurotransmission; in vivo spectroscopy

IN THE TRADITIONAL CONTEXT of neuroscience, the brain’s tasks are mainly accomplished by the neurons, with the surrounding glial cells performing simple, passive tasks of maintaining the milieu required for optimal neurotransmission. However, the glial cells are more than just passive components in neuronal function, in that they are intimately involved in the process of neurotransmission through glial uptake of glutamate (Glu) from the synaptic cleft (64, 77, 78). Glu is the major excitatory neurotransmitter (62); it is present in the mammalian brain in high concentrations and is dynamically stored in presynaptic vesicles (73). Despite the high intracellular concentration of Glu, the extracellular concentration must be maintained very low (∼0.004 mM) to avoid excitotoxicity. Presynaptic release of Glu into the synaptic cleft therefore requires efficient uptake mechanisms, which are achieved by Glu transporters (2). Most of the metabolic evidence suggests that uptake by glia is the most important process. Most of the Glu is in neurons (51), as is most of the glutaminase activity (52), whereas astrocytes contain most of the glutamine (Gln) (51), all of the glutamine synthetase (42), and pyruvate carboxylase (63); they predominantly take up and metabolize acetate (74). Early studies showed that cerebral Glu metabolism is compartmentalized, involving two major metabolic pools of Glu (7, 16, 71). The large pool has been associated with the neuronal compartment and the small pool with the glial compartment. Recent studies have again supported the participation of glia in neurotransmission through rapid clearance of Glu from the synaptic cleft into neighboring glia, on the basis of conductance currents associated with Glu uptake (6) and consequent metabolism. The uptake of Glu into the astrocytes is associated with uptake of glucose into the glial compartment (39), thereby linking stimulated energy metabolism between glial and neuronal cells during neurotransmission.

In summary, the glial-neuronal metabolic relationship mediated by Glu-Gln interconversion appears to be essential for glutamatergic neurotransmission. This compartmentation of metabolic pathways into both the glial and neuronal fractions extends to other systems as well and may represent a fundamentally important biochemical process for cerebral tissue. For instance, aspartate-like immunoreactivity was recently found to colocalize with Glu in brain slices (25), and aspartate aminotransferase stained the neuronal compartment most intensely (75).

In recent years, 13C NMR spectroscopy of brain slices (2), extracts (37, 64), and cell cultures (9, 26, 46) has corroborated and extended the initial findings of compartmentalized cerebral energy and Glu metabolism. Given the specific compartmentation of critical enzymes for cerebral energy metabolism, the use of 13C NMR spectroscopy offers an unprecedented amount of

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highly specific information (17). Such data are obtained from the amount of label incorporated into the different positions of one or more molecules after administration of a specifically labeled metabolic precursor, such as glucose, the major source of energy in brain (3, 5, 57, 68). From the specific labeling pattern, the relative and absolute fluxes through a given pathway can be calculated. For example, the incorporation of multiply labeled glucose into multiply labeled Glu at the C2 position is indicative of pyruvate carboxylase flux at low enrichment (37). The specific information gained by 13C NMR spectroscopy can also be used to estimate rates of pyruvate recycling and of malic enzyme activity (17, 47). In addition to the analysis of isotopomers (33, 40), which has been in widespread use for analyzing 13C NMR spectra of brain extracts (68), dynamic incorporation of label into a given position can be observed. Metabolic rates can be quantitatively extracted from the rate of label incorporation. These approaches require by necessity that accurate temporal data be obtained in vivo, but the derivation of metabolic rates depends more critically on the specific model used to analyze the data and the assumptions made (76). In brain, several models have been proposed, some of which have been used to calculate metabolic rates (17, 23, 44, 67, 72). Given the compartmentation of cerebral enzymes, such as glutamine synthetase, the landmark observation that Gln labeling can be detected noninvasively in the brain (19, 21, 23) is thus of crucial importance to the study of metabolic compartmentation, as pointed out in a recent review (3).

The aim of this study was to fully incorporate the maximum information achievable in vivo localized 13C NMR spectra of human brain using state-of-the-art sensitivity and methodology (20) available at 4 Tesla. The resulting measurement of label incorporation into eight distinct resonances in amino acids was predicted to provide metabolic rates that are less dependent on each other. Overall, on the basis of known cellular compartmentation of metabolism and enzymes, we sought to determine whether sufficiently specific information could be obtained from the human brain to permit assessment of cellular cerebral energy metabolism in vivo. This information can then be used further to serve as a basis for unraveling the relative contributions of both cell types to brain function in health and disease.

MATERIALS AND METHODS

Subjects. Six healthy human subjects were studied after giving informed consent according to procedures approved by the Institutional Review Board: Human Subjects Committee. On the morning of study, subjects reported to the Center for Magnetic Resonance Research (University of Minnesota) in the fasting state. In preparation for the clamp procedure, an intravenous catheter was placed antebrachial in each forearm and retrograde in a lower leg/foot. Arms and legs were warmed by placing preheated pads and water-soaked towels around the lower extremities. Somatostatin was infused into one arm vein at a progressively increasing rate up to 0.16 μg·kg⁻¹·min⁻¹ to suppress endogenous pancreatic insulin and glucagon secretion (61). Dextrose (50% wt/vol d-glucose) was infused into the other arm vein at a variable rate adjusted to maintain target glycemia at 15 mM plasma glucose concentration. The infusion procedures have been described previously (23). Alterations in the glucose infusion rate were made on the basis of plasma glucose concentration measured on a nearby glucose analyzer (Beckman, Fullerton, CA) in blood samples taken from the foot vein every 3–5 min (60). Additional blood samples were obtained every 20 min for the later determination of plasma insulin concentration, and both before and after the study for assessment of plasma ketone levels. When the subject was ready for spectroscopic study, a bolus injection of 30 g of [1-13C]glucose was given as 50% d-glucose in water, with a fractional enrichment of 99% over 1–2 min. As in our previous study (23), the plasma glucose was then clamped at the peak level of glycemia (~15 mM plasma glucose concentration) by the infusion of 10 g [1-13C]glucose (prepared as 20% d-glucose in water with a fractional enrichment of 70%) at a variable rate determined by the plasma glucose concentrations. After administration of [1-13C]glucose, additional plasma samples were collected every 10 min to be used for the determination of plasma glucose enrichment by use of gas chromatography-mass spectrometry (GC-MS).

Chemical assays and GC-MS. Insulin was measured in serum that had been frozen within 30 min of acquisition with the double-antibody method of Morgan and Lazarow (50). Plasma insulin was not detected in our study. Absence of serum ketones was verified in the clinical laboratory by a qualitative test based on the nitroferrocyanide reaction. Analyses of the 13C enrichment in serum glucose were performed by the University of Minnesota General Clinical Research Center GC/MS Core Laboratory by use of the following standard procedures. After deproteinization, the supernatants were purified by chromatography, as previously described (8). The fraction containing glucose was converted to the pentatri methylsilyle 0-methyl oxime derivative by a modification of the procedure of Laine and Sweeley (35). After the trimethylsilyl derivative was produced, analysis by GC-MS was performed on a Hewlett-Packard 5973 MSD system equipped with an HP6890 series gas chromatograph in the selective ion-monitoring mode. Ions at 160 and 161 were analyzed to determine the enrichment of 13C in carbon 1 of glucose.

13C MR spectroscopy. All studies used a 4-Tesla magnet with a 125-cm bore, equipped with a standard clinical body gradient coil and amplifier (Siemens AS25, Erlangen, Germany). The magnet and gradient system was interfaced with a spectrometer console (Varian, Palo Alto, CA) by use of a manufacturer-supplied interface board. Subjects were positioned supine on the patient bed above the surface coil. After coil tuning, MR imaging was performed to determine localization for spectroscopy according to anatomical landmarks. Subjects wore earplugs to minimize gradient noise and were placed into the coil holder with cushions to minimize head movement. Shimming of the identified region of interest was performed using FASTMAP (19), which resulted in linewidths of 7–9 Hz.

To efficiently separate the proton (169 MHz) and the 13C frequency (42.5 MHz), we used a three-coil design in which the circular polarized 1H radio frequency (RF) field was generated by two distinct 14-cm-diameter coils driven by a quadrature hybrid. The 13C coil was a single-loop 9-cm-diameter surface coil. This three-coil design was recently described elsewhere (1). Observation of the Federal Drug Administration guidelines for power absorption was verified using methods and procedures presented in detail elsewhere.
(1, 20, 23). RF power for excitation, polarization transfer, and decoupling was carefully calibrated using a small sphere containing 0.5 ml of 13C-labeled formic acid placed at the 13C coil center, as described previously (for example, see Ref. 20). These calibrations were used to ensure proper power settings for decoupling as well as to minimize RF power needed for the experiment.

Localization was performed on the longitudinal proton z-magnetization, which was transferred to the 13C magnetization using a semi-adiabatic polarization transfer method, PREt Excited Carbon-13 Image SElected in vivo Localized spectroscoPy, or PRECISELY (20), as described recently (23). Editing delays were set to correspond to a heteronuclear coupling constant of $J_{\text{CH}} = 137$ Hz.

Spectra were analyzed after 3-Hz apodization, zero-filling, and fast-Fourier transform by use of the fitting algorithm supplied by the spectrometer software. To reduce variability, linewidths of 13C-13C doublets were set to the linewidth of the corresponding center peak, and the fitted frequencies of the 13C-13C doublets were fixed to be symmetrical to the main resonance. According to the homonuclear 13C-13C coupling constants. After correction for field frequency drift, the frequencies and linewidths of the fitted peaks were determined on the basis of fit to a spectrum representing the average of 60 min of data accumulation. This procedure was justified on the basis of the observation of <3-Hz changes in 1H spectra (corresponding to <0.75-Hz changes in 13C spectra) in studies performed over similar time periods with the identical equipment. Convergence of the fit procedure was verified by inspecting the residuals of the fit point by point.

Quantification of integrated 13C signals was performed relative to the signals of N-acetyl-aspartate (NAA) at 22.7 ppm (C6) and 54.0 ppm (C2) set to correspond to 0.12 mM on the basis of our previous observation of a stable NAA C2 signal at 54.0 ppm (23). Stability of the NAA signals was verified for 2 h after start of the 1-13C glucose infusion for both the C2 and C6 resonances (data not shown). This calculation assumes that the 1H saturation factors are identical in vivo, which was supported by inversion-recovery nulled spectroscopy at 4 Tesla (49) and the relatively long repetition time of 3 s. Signal differences due to differential T2 were neglected, because the measured linewidths of 2–3 Hz implied that T2 is longer than 100 ms, which is much longer than the T2 evolution time of the sequence (9 ms).

Modeling of compartmentalized neurotransmitter metabolism in the human brain. The time courses were used as the experimental data to fit the model recently proposed in Ref. 23, which is redrawn in Fig. 1A. Because the scheme does not explicitly describe the mechanisms by which label is scrambled in the tricarboxylic acid (TCA) cycle, we have added the scheme in Fig. 1B.

The scheme in Fig. 1B explicitly accounts for potential finite exchange between the amino acids in the cytosol and the TCA cycle intermediates in the mitochondrion. The differential Eqs. 5–21 that follow are derived by the generalized procedure described in Ref. 23. Label scrambling in the amino acids due to TCA cycle activity was modeled according to the scheme in Fig. 1B, derived as a special case of the general model by Chance et al. (10).

Briefly, label derived from the C1 or C6 of glucose arrives at the C3 of pyruvate/lactate, where depending on whether the label enters the TCA cycle via pyruvate carboxylase (flux $V_{\text{PC}}$) or pyruvate dehydrogenase ($V_{\text{PDH}}$) reaction, it ultimately is detected in the C4 or C2 position of Glu. Label scrambling due to TCA cycle activity results in the C2 and C3 of 2-oxoglutarate (OG) receiving label from the C4 of OG (Fig. 1B). In neurons, $V_{\text{PC}}$ was neglected, and in astrocytes, conservation of mass required that the flux through glial pyruvate dehydrogenase be equal or larger than $V_{\text{PC}}$, which was modeled by setting the flux through glial pyruvate dehydrogenase to $V_{\text{PC}} + V_g$, with $V_g \geq 0$ (Fig. 1A), where $V_g$ accounts for the difference in flux between glial pyruvate dehydrogenase and pyruvate carboxylase.

![Diagram](image-url)
Label accumulation into Gln proceeds almost exclusively in glia because of the exclusive localization of glutamine synthetase (EC 6.3.1.2) in astrocytes (Fig. 1A).

The effect of a sizable brain glucose concentration on the isotope kinetics cannot be completely ignored (22, 43). Therefore, we calculated the enrichment of brain glucose from the measurements of plasma glucose concentration and isotopic fraction by use of the reversible Michaelis-Menten model of glucose transport, which has been shown to provide a more consistent depiction of brain glucose concentrations and transport (12, 24). The differential equation describing the change in total brain glucose \([G_{\text{brain}}(t)]\) in \(^{13}\text{C}\)-labeled brain glucose \([^{13}G_{\text{brain}}(t)]\) is given by

\[
\frac{dG_{\text{brain}}}{dt} = \frac{\text{Tmax}}{K_1 + G_{\text{brain}}(t)V_d + G_{\text{plasma}}(t)}^{13}G_{\text{plasma}}(t) - \frac{\text{Tmax}}{K_1 + G_{\text{brain}}(t)V_d + G_{\text{plasma}}(t)}G_{\text{brain}}(t) = \text{CMR}_{\text{Glc}}
\]

where \(K_1\) is the Michaelis-Menten constant of glucose transport, \(\text{Tmax}\) is the corresponding maximal transport rate, and \(\text{CMR}_{\text{Glc}}\) is glucose consumption. For a more detailed description see Ref. 24. Brain glucose is metabolized by glycolysis to pyruvate, which is assumed to be in rapid exchange with lactate, given the high activity of cerebral L-lactate dehydrogenase (EC 1.1.1.27). We assumed cerebral lactate to have the same isotopic enrichment in both cell types because of the small lactate concentration and large distribution volume (55), in agreement with a high lactate transport efficiency (47). Therefore, only one single cerebral rate of glucose consumption was taken into account; this, however, does not assume that all glycolysis occurs in glia.

The rate of label incorporation into cerebral lactate is thus a function of changing fractional enrichment of brain glucose and the metabolic rate \(\text{CMR}_{\text{Glc}}\) and the dilution/efflux \(V_{\text{out}}\) (29)

\[
\frac{d^{13}\text{Lac}}{dt} = \text{CMR}_{\text{Glc}} \frac{^{13}\text{Glc}(t)}{\text{Glc}(t)} + \text{CMR}_{\text{Glc}} \frac{^{13}\text{Glc}(t)}{\text{Glc}(t)} - 2 \text{CMR}_{\text{Glc}}(\text{app}) + V_{\text{out}} \frac{^{13}\text{Lac}(t)}{\text{Lac}} + V_{\text{out}} \text{FE}_{\text{Lac}}
\]

This equation assumes that \(V_{\text{out}}\) models the exchange of label with unlabeled plasma lactate, whose fractional enrichment is given by \(\text{FE}_{\text{Lac}}\). It was assumed to be 0.011 in this study. \(\text{CMR}_{\text{Glc}}\) was set to 0.45 m mol g\(^{-1}\) min\(^{-1}\), and oxidized \(\text{CMR}_{\text{Glc}}\) \(\text{CMR}_{\text{Glc}(\text{ox})}\) was set to 0.97 \(\text{CMR}_{\text{Glc}}\). Equations 1–3 were solved using a fourth-order Runge-Kutta algorithm based on the measured time course of plasma glucose and its fractional enrichment, yielding the time course of fractional enrichment for lactate C3, Lac3(\(t\))/Lac.

\(V_{\text{out}}\) is assumed to be equivalent to label dilution due to pentose phosphate shunt activity and label dilution at the lactate level (32) and, in principle, also at the acetyl-CoA level. Because the brain relies almost entirely on glucose for energy metabolism, and because fatty acid uptake is small and ketone bodies were not detected in our study, we assumed that dilution at the acetyl-CoA level in brain is negligible. Net loss of lactate can be modeled by assuming \(V_{\text{Lout}} = V_{\text{out}}\). In the resting brain, \(V_{\text{Lout}} \sim V_{\text{out}}\), or almost complete oxidative metabolism of glucose, defined as \(2 \text{CMR}_{\text{Glc}} = 2 \text{CMR}_{\text{Glc}(\text{ox})} - V_{\text{Lout}} + V_{\text{out}}\).

In our scheme (Fig. 1A), total \(\text{CMR}_{\text{Glc}(\text{ox})}\) (defined as the rate of glucose equivalents entering the TCA cycle) is related to the fluxes in glial and neuronal TCA cycles by the relationship

\[
\text{CMR}_{\text{Glc}(\text{ox})} = \frac{V_{\text{PDH}} + V_s}{2} + \text{PC}
\]

where \(V_s\) denotes the flux through glial pyruvate dehydrogenase corresponding to complete oxidation of pyruvate, i.e., \(V_s + \text{PC}\) is the total flux through glial pyruvate dehydrogenase (as outlined in the scheme in Fig. 1A). \(V_{\text{PDH}}\) is the analogous flux in neurons, and \(\text{PC}\) is the rate of net oxaloacetate (OAA) and net citrate formation (anaplerosis). The net carbon compound formed is in our steady-state model removed by net consumption of OAA and biosynthesis of Gln.

Throughout this section, the superscript 13 denotes the \(^{13}\text{C}\) label, and the numeral subscripts indicate the position at which the label is observed, e.g., \(^{13}\text{Glu}\) denotes the sum of all isotopomers of Glu with \(^{13}\text{C}\) label at the C4 position. The derivation of these and the following differential equations follows from tracer kinetics and is mathematically equivalent to the procedure outlined previously (23) and used in many earlier studies (10, 14, 40, 57).

Because the gluconeogenic capacity, as well as the capacity to generate pyruvate or lactate from amino acids, is generally small in the neuronal compartment (38), we assumed that the net flux of Glu carbon skeletons into the neuronal TCA cycle was negligible compared with \(V_{\text{PDH}}\).

The NMR signal represents total tissue Glu concentration, and Gluq, conversely, of which the vesicular neurotransmitter pool is generally viewed to constitute a small fraction. Neglecting the contribution of extracellular Glu (0.004 m mol g\(^{-1}\)) to the NMR signal, the neuronal Glu pool [Glu\(^{(n)}\)] can be partitioned into a vesicular (small) neurotransmitter signal Glu\(^{\text{NT}}\) plus a metabolic pool Glu\(^{\text{met}}\). Based on studies showing 1) rapid redistribution of label between vesicular and extravascular Glu (73), 2) that isolation of Glu-containing vesicles requires rapid isolation procedures (58), and 3) that influx of Glu results in simultaneous efflux of Gln from glial cells (34, 48), we assumed that the exchange between Glu\(^{\text{met}}\) and Glu\(^{\text{NT}}\) is rapid compared with \(V_{\text{PDH}}\). The rate of Glu flux from the astrocyte to the glutamatergic neuron. For definitions of symbols, see also Fig. 1A. In this case, the label incorporation into the observed Glu signal will reflect the label incorporation into the neurotransmitter Glu pool, Glu\(^{\text{NT}}\).

The lack of metabolic pathways branching off at the level of neuronal Glu, or Glu\(^{(n)}\), and the metabolic steady-state requirement that no net concentration changes occur, e.g., dGlu\(^{(n)}\)/dt = 0, imply that the rate across the glial-neuronal interface be \(V_{\text{PDH}}^{\text{app}}\). Under these assumptions, the rate of unidirectional Glu transport out of the neuron is equal to \(V_{\text{PDH}}^{\text{app}}\), and the rate of OG and \(^{13}\text{Glu}\)\(^{(n)}\) labeling can be written, accordingly, as

\[
\frac{d^{13}\text{OG}(t)}{dt} = V_{\text{PDH}}^{\text{app}} \frac{^{13}\text{Lac}(t)}{\text{Lac}} - (V_{\text{PDH}} + V_s) \frac{^{13}\text{OG}(t)}{\text{OG}(t)} + V_s \frac{^{13}\text{Glu}(t)}{\text{Glu}(t)}
\]
d\(^{13}\text{Glu}_4^n(t)\)/dt = \(V_{x}^{\text{OG}_4^n(t)}\) \(\text{OG}_4^n\) - (\(V_{x} + V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\)) \(\text{OG}_4^n\) + \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\) \(\text{OG}_4^n\) (6)

\[
\frac{d\bar{\text{OG}}_3^n}{dt} = \frac{V_{\text{PDH}}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} - (V_{\text{PDH}} + V_{x}) \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} + \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} (7)
\]

\[
\frac{d\text{13Glu}_3^n}{dt} = \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} - (V_{x} + V_{\text{Glu}_3^n}^{\text{OG}_3^n(t)} \text{OG}_3^n) + \frac{V_{\text{Glu}_3^n}^{\text{OG}_3^n(t)} \text{OG}_3^n}{\text{Glu}_3^n} (8)
\]

By equating the forward and backward exchange rates between Glu and OG, we have assumed that net flux of neuronal Glu into the neuronal TCA cycle is negligible compared with the unidirectional exchange rates (\(V_{x}\)) that describe the exchange rate between (mitochondrial) OG (and (cytosolic) Glu (see also Fig. 1). Therefore, \(V_{x}\) is a composite figure that describes the combined effect of glutamate dehydrogenase, aspartate transaminase, and transport across the mitochondrial membranes. Given the slow incorporation of nitrogen into Glu compared with the glutamine amide group (15), glutamate dehydrogenase flux must be small compared with the flux through glutamine synthetase; it was, therefore, neglected. This assumption is also consistent with studies showing a reduced Glu concentration when aspartate transaminase was inhibited (11). The differential equations for \(\text{Glu}_4^n\) are equivalent to those for \(\text{Glu}_4^n\) and are simply derived by replacing the subscript. Likewise, analog equations can be written for \(\text{Glu}_2^n\) simply by replacing the subscript. Label incorporation into OAA, which is in exchange with Asp, is described by the following equations

\[
\frac{d\bar{\text{OG}}_3^n}{dt} = \frac{V_{\text{PDH}}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} - (V_{\text{PDH}} + V_{x}) \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} + \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} (9)
\]

\[
\frac{d\text{13Glu}_3^n}{dt} = \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} - (V_{x} + V_{\text{Glu}_3^n}^{\text{OG}_3^n(t)} \text{OG}_3^n) + \frac{V_{\text{Glu}_3^n}^{\text{OG}_3^n(t)} \text{OG}_3^n}{\text{Glu}_3^n} (10)
\]

\[
\frac{d\text{13Asp}_3^n}{dt} = \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} - \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13Asp}_{3}^{n}(t)}{\text{Asp}_{3}^{n}} (11)
\]

\[
\frac{d\text{13Asp}_3^n}{dt} = \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13OG}_{3}^{n}(t)}{\text{OG}_3^n} - \frac{V_{x}}{\text{OG}_3^n} \frac{\text{13Asp}_{3}^{n}(t)}{\text{Asp}_{3}^{n}} (12)
\]

The lack of metabolic pathways branching off at neuronal Gln was based on observation of little or no Glu efflux into the medium of cultured neurons, as shown in, for example, Ref. 38. The rate of change in \(\text{Glu}_4^n\) is thus given by

\[
\frac{d\text{13Glu}_4^n}{dt} = \frac{V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}}{\text{Glu}_4^n} - \frac{V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}}{\text{Glu}_4^n} (13)
\]

and likewise for the other positions in Gln (\(\text{Glu}_3^n\)), because the glutaminase reaction does not change the positional \(13\text{C}\) labeling between Gln and Glu.

Glial metabolism: glutamine synthetase and pyruvate carboxylase. In reference to the majority of evidence that links the Glu/Gln interrelationship to excitatory neurotransmission (77), we have denoted the rate from Gln (\(\text{Gln}_4^n\)) to Glu (\(\text{Glu}_4^n\)) and from Glu (\(\text{Glu}_4^n\)) to Glu (\(\text{Glu}_4^n\)) as \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\), the apparent rate of neurotransmission. In view of the low glutaminase (EC 3.5.1.2) activity in glia (28), we assumed that the glutaminase rate \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\) is negligible compared with \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\). Although we assumed in this study that \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)} = 0\) (as indicated by the dashed arrow in Fig. 1A), the equations below are written to allow for some \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\).

The steady-state requirement

\[
\text{V}_{\text{Glu}_4^n}^{\text{OG}_4^n(t)} = V_{\text{PC}} + V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)} + V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)} (14)
\]

assumes that anaplerosis leads to glial loss of Gln. Loss of Gln from the glial cell to the extracellular space is, in this case, modeled by the term \(\text{V}_{\text{efflux}} = V_{\text{PC}}\). The rate of \(\text{Glu}_4^n\) labeling is thus given by

\[
\frac{d\text{13Glu}_4^n}{dt} = \frac{V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}}{\text{Glu}_4^n} - \frac{V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}}{\text{Glu}_4^n} (14)
\]

and equivalent equations can be written for the 2 and 3 positions of glial Gln simply by replacing the subscript 4 with 2 and 3, respectively

\[
\frac{d\text{13Glu}_2^n}{dt} = \frac{V_{\text{Glu}_2^n}^{\text{OG}_2^n(t)}}{\text{Glu}_2^n} - \frac{V_{\text{Glu}_2^n}^{\text{OG}_2^n(t)}}{\text{Glu}_2^n} (15)
\]

\[
\frac{d\text{13Glu}_3^n}{dt} = \frac{V_{\text{Glu}_3^n}^{\text{OG}_3^n(t)}}{\text{Glu}_3^n} - \frac{V_{\text{Glu}_3^n}^{\text{OG}_3^n(t)}}{\text{Glu}_3^n} (16)
\]

In addition to label derived from neuronal Glu (\(\text{Glu}_4^n\)), label can be incorporated into glial glutamate (\(\text{Glu}_4^n\)) from the glial TCA cycle, the rate of which is given by \(V_{\text{Glu}_4^n}^{\text{OG}_4^n(t)}\) (Fig. 1). Pyruvate carboxylase (PC, EC 6.4.1.1) transfers label from pyruvate C3 to OAA C3 in the glial compartment. In this model, reverse flux from OAA to fumarate was neglected, on the basis of previous reports suggesting a substantial difference in labeling at the C1 and C4 position of OAA (31), which is supported by differential labeling of Glu C2 and C3 in astrocytes (41). Neglecting any backflux to fumarate underestimates the pyruvate carboxylase flux when assessed from the differential labeling of the C2 and C3 positions in Glu and Gln. Given the small pool size of cerebral OAA and most TCA cycle intermediates, label equilibration is assumed to be relatively fast until it reaches OG. The small pool size of glutamate (\(\text{Glu}_4^n\)) relative to the high activity of the malate-aspartate shuttle is assumed to result in rapid label equilibration of glutamate (\(\text{Glu}_4^n\)) relative to OAA (\(\text{Glu}_4^n\)). \(\text{Glu}_4^n\) is also labeled from neuronal Glu (\(\text{Glu}_4^n\)) as well as from glial \(\text{Glu}_4^n\) on subsequent turns of the TCA cycle.
were assumed to be constant during the duration of the OAA labeling.

Less dependent on the exchange apodization (3 Hz) and is shown without baseline correction.

\[
\frac{d^{13}OAA^g}{dt} = (V_g + V_{PC}) \frac{^{13}\text{Lac}_0(t)}{\text{Lac}} - (V_g + V_{PC} + V_x) \frac{^{13}OAA^g(t)}{\text{OG}^g} + V_x \frac{^{13}\text{Glu}^g(t)}{\text{Glu}^g} + V_g \frac{^{13}\text{Gln}^g(t)}{\text{Gln}^g} + V_{\text{ex}} \frac{^{13}\text{Glu}^g(t)}{\text{Glu}^g} + V_{g\text{app}} \frac{^{13}\text{Gln}^g(t)}{\text{Glu}^g}
\]

\[
\frac{d^{13}\text{Glu}^g}{dt} = V_x \frac{^{13}OAA^g(t)}{\text{OG}^g} - (V_x + V_{\text{ex}}) \frac{^{13}\text{Glu}^g(t)}{\text{Glu}^g}
\]

\[
\frac{d^{13}OAA^g}{dt} = V_{PC} \frac{^{13}\text{Lac}_0(t)}{\text{Lac}} + \frac{V_g}{2} \frac{^{13}OAA^g(t)}{\text{OG}^g} - (V_g + V_{PC}) \frac{^{13}OAA^g(t)}{\text{OG}^g} + \frac{V_x}{2} \frac{^{13}OAA^g(t)}{\text{OG}^g} - (V_g + V_{PC} + V_x) \frac{^{13}OAA^g(t)}{\text{OG}^g} + V_x \frac{^{13}OAA^g(t)}{\text{OG}^g}
\]

\[
\frac{d^{13}OAA^g}{dt} = (V_g + V_{PC}) \frac{^{13}OAA^g(t)}{\text{OG}^g}
\]

\[
\frac{d^{13}\text{Glu}^g}{dt} = V_x \frac{^{13}OAA^g(t)}{\text{OG}^g} - (V_x + V_{\text{ex}}) \frac{^{13}\text{Glu}^g(t)}{\text{Glu}^g}
\]

Numerical procedures. The cerebral Glu\(^{(g)}\) + Glu\(^{(n)}\) pool size labeled by \(^{13}\text{C}\)glucose was estimated at 5.7 μmol/g, in agreement with previous studies (53, 54, 56), from the amount of \(^{13}\text{C}\)labeled Glu signal divided by the fractional enrichment determined from the \(^{13}\text{C}\)-\(^{13}\text{C}\) isotopomers as described previously (21, 37, 40). Likewise, the cerebral aspartate pool was estimated at 1.5 μmol/g, and this neurotransmitter was assumed to be mainly in the neuronal compartment.

The set of differential equations (see Eqs. 5–21) was solved, and \(^{13}\text{Glu}^{(n)} + \text{Glu}^{(n)}\) and \(^{13}\text{Glu}^{(n)} + \text{Gln}^{(n)}\) were simultaneously fitted using commercially available software (SAAM II, The SAAM Institute, Seattle, WA) to the separately measured time courses of Glu C4 and Glu C4 as well as the C2 and C3 positions. In addition, we included the combined signal of Asp C2 and C3 in the modeling, Asp\(_{\text{pool}}\), because the smaller pool size of Asp makes the labeling curve less dependent on the exchange \(V_x\) compared with the rate of OAA labeling.

All metabolite pools [except for cerebral glucose (Glc\(_{\text{brain}}\)] were assumed to be constant during the duration of the \(^{13}\text{C}\)glucose infusions: 14% of the total glutamate pool was assumed to be in the glial compartment; see Ref. 17 and references therein. Consistent with most evidence (51), we assumed that the neuronal Glu, Glu\(^{(n)}\), was small (e.g., 0.2 μmol/g), and we verified that this assumption did not influence substantially the labeling time course of Glu. The glutamine pool, Glu\(^{(n)} + \text{Gln}^{(n)}\), turned over by \(^{13}\text{C}\)glucose metabolism, was estimated at 1.7 μmol/g with the same methods as for Glu. We assumed cerebral OG and OAA pools to be very small, i.e., OG\(^{(n)}\) = OG\(^{(g)}\) = OAA\(^{(n)}\) = OAA\(^{(g)}\) = 0.1 μmol/g. The cerebral lactate pool was set to a fixed value of 1.0 μmol/g. The pool sizes of other glycolytic and TCA cycle intermediates were also assumed to be small and without effect on isotope kinetics; they were validated to be without effect on the conclusions of this paper up to a total mass of several micromoles per gram. On the basis of our inability to detect signals from TCA cycle intermediates, even when summing spectra over extended measurement periods from all measured subjects, we assumed the pool sizes to be below 0.05 μmol/g, which we verified to have a negligible impact on the calculated fluxes (not shown).

The following rates were varied to achieve the best fit to the data: \(V_{\text{PDH}}\), \(V_x\), \(V_{\text{out}}\), \(V_{\text{NT}}\), \(V_{\text{g}}\), \(V_{\text{PC}}\). All fluxes were constrained to be positive in the fitting process. To take into account that the malate-aspartate shuttle is the major mechanism by which the brain maintains the cytosolic redox state under normoxic conditions, we constrained the exchange rate \(V_x\) to be equal or greater than the pyruvate dehydrogenase flux, \(V_{\text{PDH}}\).

RESULTS

The improved sensitivity achieved at 4 Tesla was used to reduce the volume of interest being investigated and to achieve localization to a metabolically more homogenous area in the human brain. Figure 2 illustrates the excellent sensitivity achieved with our approach. The spectrum was acquired 1 h after the start of \(^{13}\text{C}\)glucose infusion and represents data collection corresponding to 45 min from a volume of 45 ml. In addition to the three dominant resonances from Glu, resolved peaks were detected from the corresponding three positions in Glu, and resonances from NAA and GABA were routinely observed. Furthermore, the resolution and sensitivity afforded the simultaneous detection of label incorporation into cytosolic amino acids in a 45-ml volume in the human occipital lobe at 4 Tesla. This is a representative spectrum obtained from a \(3 \times 3 \times 5\)-cm\(^3\) volume in the human visual cortex in 45 min. Resonance assignments are as follows: Glu C2 at 55.6 ppm, Glu C2 at 55.0 ppm, N-acetyl-aspartate (NAA) C2 at 54.0 ppm, Asp C2 at 53.7 ppm, NAA C3 at 40.5 ppm, GABA C4 at 40.45 ppm, Asp C3 at 37.6 ppm, GABA C2 at 35.3 ppm, Glu C4 at 34.2 ppm, Gln C4 at 31.7 ppm, Glu C3 at 28.0 ppm, and Gln C3 at 27.7 ppm. In addition to these resonances, those ascribed to the homonuclear \(^{13}\text{C}\)-\(^{13}\text{C}\) coupling were readily detected at positions of all Glu resonances (brackets). The spectrum was processed with a mild Lorentz-to-Gauss apodization (3 Hz) and is shown without baseline correction.
their mitochondrial TCA cycle counterparts. This exchange is mediated by the malate-aspartate shuttle (Fig. 3A), which provides a mechanism by which Asp and Glu can be labeled from the TCA cycle through transport of Asp and Glu by the Asp/Glu antiporters (11, 36). On the basis of this mechanism, we analyzed the exchange between Asp and OAA as well as between Glu and OG with a single reaction rate, $V_x$. The use of the label incorporation into the amino acids ideally assumes that the rate of label incorporation into the cytosolic amino acids is a good approximation of label incorporation into the metabolic counterpart, e.g., OG in the mitochondrion. However, as stated previously, this assumption generally is true only when the exchange between OG and Glu is fast compared with the TCA cycle flux ($45 \times 10^5$). In addition, as shown in Fig. 3B, the accuracy by which the amino acid represents the label incorporation into the TCA cycle intermediate also depends on the relative pool sizes. For example, Asp, whose concentration is at least three times less than that of Glu, much more closely represents the fractional enrichment of OAA (dotted curves in Fig. 3B) at an otherwise equal relative rate $V_x/V_{PDH}$, whereas Glu labeling is a much poorer indicator of the corresponding OG labeling (solid curves in Fig. 3B). The effect of assuming widely varying $V_x$ had a quantitatively negligible impact on calculating the TCA cycle flux from the measurement of Asp C2+C3 (Asp$_{23}$) alone (second column in Table 1). On the other hand, the measurement from Glu C4 (Glu$_4$) alone illustrates a more profound effect of the assumed value of $V_x$ on the derived TCA cycle flux, as shown in the third column of Table 1.

The model proposed in Ref. 23 and shown in the scheme in Fig. 1A was fitted to the curves showing label incorporation into Glu C4, C3, and C2 as well as Gln C2, C3, and C4 and Asp C2 and C3 (Fig. 4). The fits resulted in a covariance matrix whose normalized off-diagonal elements were in magnitude $<0.6$ for all but one element. The resulting fitted fluxes are shown in Table 2, along with the normalized covariance matrix in Table 3. Because glucose is the dominant fuel for generation of energy in brain, the fitting was constrained, in that $V_x$ was not allowed below the minimum required flux by the malate-aspartate shuttle.

![Fig. 3](https://example.com/fig3.png)

**Fig. 3.** A: fluxes participating in the malate-aspartate shuttle (adapted from Stryer). The overall flux between mitochondrial OG/OAA and cytosolic Asp/Glu is modeled by $V_x$. B: to illustrate that the pool size does affect the fidelity by which the corresponding amino acid reflects the rate of labeling of its corresponding TCA cycle intermediate, the label in Asp relative to OAA (dotted curves) was compared with the label in Glu C4 relative to OG C4 (solid curves) for $V_x = 5.7$ and 0.55 $\mu$mol.g$^{-1}$.min$^{-1}$, assuming $V_{PDH} = 0.7$ $\mu$mol.g$^{-1}$.min$^{-1}$. Concentrations of the participating amino acids were assumed in this simulation to be 5.7 $\mu$mol/g for Glu and 1.5 $\mu$mol/g for Asp.

<table>
<thead>
<tr>
<th>$V_x$ (µmol.g$^{-1}$.min$^{-1}$)</th>
<th>Asp$_{23}$</th>
<th>Glu$_4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$57 \times 10^5$</td>
<td>1.04</td>
<td>0.53</td>
</tr>
<tr>
<td>$10 \times 10^5$</td>
<td>1.04</td>
<td>0.55</td>
</tr>
<tr>
<td>$2 \times 10^5$</td>
<td>1.03</td>
<td>0.65</td>
</tr>
<tr>
<td>$1 \times 10^5$</td>
<td>1.01</td>
<td>0.83</td>
</tr>
<tr>
<td>$0.75 \times 10^5$</td>
<td>1.00</td>
<td>1.00</td>
</tr>
</tbody>
</table>

Tricarboxylic acid (TCA) cycle flux ($V_{PDH}$) as a function of the exchange rate ($V_x$) measured from the C2 and C3 of aspartate (Asp$_{23}$) and the C4 of glutamate (Glu$_4$). $V_{PDH}$ is obtained by fitting the flux of dilution/efflux and that of pyruvate dehydrogenase, but keeping other fluxes fixed at values reported in Table 2 and dividing them by $V_{PDH}$ obtained at $V_x = 0.75 \mu$mol.g$^{-1}$.min$^{-1}$. *Value previously published in Ref. 45.
which was assumed to be $V_{PDH}$, where the fitting process converged.

Provided that flux through glutamine synthetase is exclusively due to the flux from neuronal Glu (n), Gln should be equally labeled relative to Glu at each carbon atom. Table 4 shows the relative amount of $^{13}$C NMR signal at the C2, C3, and C4 positions determined 60–120 min after the start of the glucose infusion, which was found to be measurably higher at the C2 compared with the C3 and C4 positions ($P < 0.01$). In addition to the different isotopomer populations in Gln relative to Glu, fitting to the label incorporation curves also indicated a substantial contribution of pyruvate carboxylase to the total flux through glutamine synthetase.

**DISCUSSION**

In the present study we have for the first time comprehensively measured and analyzed multiple curves of label incorporation into resonances from three different amino acids in the human brain. The inclusion of the amino acid Asp with a much lower concentration than Glu helped to reduce the mathematical covariance between fitted fluxes compared with that present in previous studies (45, 76), as judged from Table 3 and Fig. 3B. Even higher sensitivity can be obtained, for example by higher static field strength (such as 7 Tesla) and by increasing the fractional enrichment of the amino acids through the use of multiply labeled glucose, e.g., $[1,6-^{13}$C$_2]$glucose. It should then be possible to achieve much more robust measures of TCA cycle flux than through the measurement from Glu alone, as suggested by the comparisons presented in Fig. 3B and Table 1. Nevertheless, some of the advances presented in this study were achieved on the basis of the improved sensitivity afforded by the use of a human 4-Tesla system. The sensitivity shown in Fig. 2 obtained from a 45-ml volume in 45 min is comparable to that of a 144-ml volume at 2.1 Tesla in 60 min (65). This illustrates the substantial gain in sensitivity (approximately threefold) achieved at 4 Tesla compared with 2.1 Tesla. The reduced volume size measured in this study currently is the smallest reported for this type of experiment. Thus partial volume effects were smaller because of a higher contribution of gray matter to the overall signal. In addition to the size, the location of the voxel assured that signals were acquired predominantly from gray matter, consistent with the very high cerebral blood flow and the high metabolic glucose consumption rate measured by fluorodeoxyglucose and $[^{11}$C]glucose positron emission tomography (PET) in this region (70). Furthermore, $^1$H MRS (59) consistently showed a choline-to-creatine ratio associated with a predominantly gray matter composition of the human occipital lobe (unpublished data), according to Hetherington et al. (27). We therefore assumed that interindividual differences in tissue composition were minimized for the volumes used in the present study.

Our study indicates a rate of neuronal TCA cycle flux ($V_{PDH}$, Fig. 1A) of 0.57 μmol·g$^{-1}$·min$^{-1}$ (Table 2). The small but measurable glial pyruvate dehydrogenase flux, $V_{PC} + V_{g}$, is consistent with active glial metabolism of acetate (74). Incorporating the small glial TCA cycle flux rate of 0.06 μmol·g$^{-1}$·min$^{-1}$ and the rate of pyruvate carboxylase, $V_{PC}$, of 0.09 μmol·g$^{-1}$·min$^{-1}$, an oxidative glucose consumption rate [CMR$_{Glc(oxy)}$] of 0.41 ± 0.03 μmol·g$^{-1}$·min$^{-1}$ was derived, which is in excellent agreement with PET measurements of total CMR$_{Glc}$ in resting gray matter (70) and the nearly complete oxidation of cerebral glucose under resting conditions.

**Table 2. Derived metabolic fluxes**

<table>
<thead>
<tr>
<th>$V_{PDH}$</th>
<th>$V_{s}$</th>
<th>CMR$_{Glc(oxy)}$</th>
<th>$V_{NT}$</th>
<th>$V_{PC}$</th>
<th>$V_{g}$</th>
<th>$V_{out}$</th>
<th>$V_{syn}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.57 ± 0.06</td>
<td>0.57 ± 0.19</td>
<td>0.41 ± 0.03</td>
<td>0.17 ± 0.05</td>
<td>0.09 ± 0.02</td>
<td>0.06 ± 0.04</td>
<td>0.41 ± 0.04</td>
<td>0.26 ± 0.06</td>
</tr>
</tbody>
</table>

Metabolic fluxes (μmol·g$^{-1}$·min$^{-1}$) with reference to model shown in Fig. 1A; see definitions of fluxes in legend to Fig. 1.
In principle, the metabolic relationship between Glu and Gln implies that the relative distribution of label in the different positions of Gln must be the same as that of Glu, with the assumption that the large (neuronal) pool is the dominant source of label for the (glial) pool of Gln. Any differential extent of labeling in brain Gln therefore implies that other, glial, reactions, such as pyruvate carboxylase, must contribute significantly to the flux through glutamine synthetase. In this investigation, we extended our previous work to measure pyruvate carboxylase activity in the human brain by use of a single, isotopically enriched substrate that can be obtained at comparatively low cost, namely d-[1-13C]glucose. Our measurement is in excellent agreement with previous studies using d-[U-13C6]glucose (37) and our previous report from larger volumes in the human brain (23). The 95% confidence interval for the rate of pyruvate carboxylation in this and our previous study (23) overlaps well with the upper limit of a more recent study, which assessed the rate of anaplerosis from the Glu C4 and Gln C4 resonances only (65). However, when label incorporation is measured into only one or two positions, the complexity of cerebral energy metabolism is likely to result in ambiguous numerical solutions because four different fluxes were simultaneously fitted. Consequently, the previous assertion of a very small activity of pyruvate carboxylase must be considered with caution.

It should be stressed in this context that our modeling does not assume that the rate of pyruvate carboxylation must result in a net loss of Glu into the bloodstream. Because Gln is the single most concentrated amino acid in the cerebrospinal fluid, it can be metabolized by many other reactions and compartments. Regardless of the specific quantitative value of pyruvate carboxylation, the consistent observation that isotopomers of Glu and Gln are not identical suggests that the Glu/Gln interconversion is not the sole source of flux through glutamine synthetase, in that pyruvate carboxylation can contribute substantially to the labeling pattern in glial Gln. In fact, our study suggests that the flux from (neuronal) Glu to (glial) Gln is only on the order of 41 ± 14% of the oxidative glucose consumption, which is much lower than the 1:1 stoichiometric relationship that has been claimed on the basis of analysis of C4 time courses only in whole rat head studies (67). It should also be emphasized that pyruvate carboxylation that leads to net formation of Glu, and eventually Gln, is energetically favorable, because each Gln molecule synthesized from glucose via pyruvate carboxylase (one-half of the glucose is used in the form of pyruvate for formation of OAA; the other one-half is used for the formation of acetyl-CoA needed for the net formation of citrate required to generate the extra OG required for the net synthesis of Gln) generates a total of 4 NADH molecules (two are produced by glycolysis, one by pyruvate dehydrogenase, and one by isocitrate dehydrogenase, and two ATP are formed by glycolysis and two are used by PC and glutamine synthetase), resulting in a net formation of ~10 ATP molecules (assuming a P/O ratio of 2.5), thereby removing two NH3, which is an energetically highly favorable reaction compared with the purely anaerobic combustion of glucose. Including the glial TCA cycle flux of Vg = 0.06 μmol·g−1·min−1 (Table 2), we calculate an oxidative ATP production of Vg × 32 + VPC × 10, which represents 87 ± 5% of the glial ATP generation, because the term CMRGl × 2 is added when we assume that all of the glycolysis is confined to the glial compartment. This calculation results in 3 μmol·g−1·min−1 of ATP produced in the glial compartment, a rate that can easily sustain the energy requirements for maintaining glutamatergic neurotransmission by removal of extracellular Glu via energy-dependent Glu transporters (39), because the VNT of 0.17 μmol·g−1·min−1 (Table 2) requires ~0.35 μmol·g−1·min−1 of ATP for glutamine synthetase and the Na-K pump. An important consequence of the measured energetics is that it underlines the importance of coupled glial energy metabolism to that in neurons, as previously pointed out by Magistretti et al. (39). However, it also stresses the importance of oxidative metabolism, in that even minor fluxes in oxidative glucose combustion can easily produce more ATP than the much larger flux through glycolysis, even in glia (18).

In neurons, if glial lactate is assumed to be the major energy source, the rate of neuronal ATP generation (i.e., 30 × VPDH) is 17 μmol·g−1·min−1, suggesting that, although glial oxygen consumption is significant, it is a minor component of total brain oxygen consumption, contributing one-fifth to one-seventh of the oxygen consumption measured by 13C MRS.

Table 3. Average normalized covariance matrix for fluxes derived in Table 2

<table>
<thead>
<tr>
<th>VNT</th>
<th>Vout</th>
<th>Vg</th>
<th>VPC</th>
<th>VPDH</th>
<th>Vs</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.00</td>
<td>-0.09±0.12</td>
<td>-0.35±0.18</td>
<td>-0.27±0.18</td>
<td>0.31±0.15</td>
<td>0.27±0.11</td>
</tr>
<tr>
<td>1.00</td>
<td>0.38±0.17</td>
<td>1.00</td>
<td>0.39±0.14</td>
<td>0.52±0.26</td>
<td>-0.32±0.17</td>
</tr>
<tr>
<td>1.00</td>
<td>0.79±0.03</td>
<td>1.00</td>
<td>0.79±0.03</td>
<td>-0.54±0.15</td>
<td>-0.54±0.10</td>
</tr>
<tr>
<td>1.00</td>
<td>-0.39±0.24</td>
<td>1.00</td>
<td>-0.39±0.24</td>
<td>-0.27±0.34</td>
<td>-0.27±0.34</td>
</tr>
<tr>
<td>1.00</td>
<td>0.03±0.26</td>
<td>1.00</td>
<td>0.03±0.26</td>
<td>0.25±0.26</td>
<td>0.25±0.26</td>
</tr>
</tbody>
</table>

Table 4. Relative label incorporation into Gln relative to Glu at the respective position

<table>
<thead>
<tr>
<th></th>
<th>C2</th>
<th>C3</th>
<th>C4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gln/Glu</td>
<td>0.41±0.02</td>
<td>0.28±0.04*</td>
<td>0.30±0.01*</td>
</tr>
</tbody>
</table>

Values are means ± SE; n = 6. *P < 0.01 vs. ratio measured at the C2 position.
Ideally, it is desirable to have a sufficiently large metabolic pool directly associated with the metabolic reactions, as is the case, e.g., for lactate in tumors (69). In the case of the TCA cycle, however, it appears that mitochondrial TCA cycle intermediates are below detectability in vivo. This requires the detection of isotope kinetics via the amino acids, which are in exchange with the TCA cycle intermediates. Of critical importance in this regard is the delay by which the isotope labeling kinetics of the (cytosolic) amino acid lag behind those of the associated (mitochondrial) TCA intermediate. Consider, for instance, the two pairs OAA/Asp and OG/Glu: it is clear that the rate of exchange $V_x$ relative to the pool size dictates to what extent the isotope kinetics in the amino acid reflect those of the associated intermediate. Hence, for a given $V_x$, Asp kinetics approximate those of OAA approximately four times faster than the kinetics of Glu mimic those of OG (Fig. 3B) because of the approximately fourfold lower Asp pool size.

Previous studies have focused on the question of whether the rate of label exchange between cytosolic Glu and mitochondrial OG is fast compared with the TCA cycle rate, $V_{PDH}$ (44, 45, 66, 76). In the heart, this ratio was shown to vary and to be closer to 1 (66, 76). This appears also to be the case in skeletal muscle (30). In contrast, a report in brain estimated $V_x$ at 57 $\mu$mol·g$^{-1}$·min$^{-1}$ (44, 45). Such a high rate of exchange of negatively charged OG or Glu represents a rather high rate of exchange of ions that must occur in the presence of the electrochemical gradient.

Our exchange rates are clearly lower than those reported in Refs. 44 and 45, which were based on early studies performed in the late 1980s and early 1990s. For example, the measurements were performed in large volumes encompassing a significant fraction of the brain. Because of the complexity of the modeling and scarcity of experimental detail in these early studies and differences in modeling, it is difficult to pinpoint exactly the reason why our results are much lower. The early modeling studies in brain apparently did not involve simultaneous fitting of all measured time courses, as judged from the absence of a covariance matrix or discussion thereof, and from the absence of a described total cost function. Furthermore, the sensitivity of the TCA cycle flux on the precise value of $V_x$ has not been reported in brain. As pointed out by others (76), the assessment of $V_x$ from Glu results in a large covariance between $V_{PDH}$ and $V_x$, and this covariance may have contributed to some numerical inaccuracy. In contrast, our simulations shown in Table 1 suggest that the measurement of Asp-labeling kinetics alone can greatly reduce the influence of $V_x$ on the measured TCA cycle rate. Therefore, the measurement of Asp kinetics allows in the fitting process a rather robust measurement of the TCA cycle rate, which (once known) allows a more precise measurement of $V_x$. A similar approach has been applied in the heart, where oxygen consumption measurements were combined with Glu turnover to achieve excellent quantification of $V_x$ by elimination of the large numerical covariance (76), whereas in Refs. 44 and 45, the reported errors in $V_x$ are high.

The exchange between OG and Glu on one hand and between Asp and OAA on the other hand is also an integral component of the malate-aspartate shuttle, which transports the two NADH produced by oxidative glycolysis into the mitochondrion to maintain the cytosolic redox potential (Fig. 3B). Therefore, we also incorporated Asp labeling in our analysis, in addition to Glu and Gln. The resulting exchange rate had a skewed error distribution to higher values but was statistically not different from the theoretical mini-

### Table 5. Sensitivity of $V_{NT}$, $CMR_{Glc(oxy)}$, $V_G$, $V_{PDH}$, and $V_{PC}$ on the assumed cellular distribution of glutamate

<table>
<thead>
<tr>
<th>$\alpha^*$</th>
<th>$V_{PDH}$</th>
<th>$CMR_{Glc(oxy)}$</th>
<th>$V_{NT}$</th>
<th>$V_{PC}$</th>
<th>$V_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.033</td>
<td>0.60 ± 0.06</td>
<td>0.41 ± 0.03</td>
<td>0.25 ± 0.07</td>
<td>0.09 ± 0.02</td>
<td>0.03 ± 0.04</td>
</tr>
<tr>
<td>0.1</td>
<td>0.58 ± 0.06</td>
<td>0.41 ± 0.03</td>
<td>0.20 ± 0.06</td>
<td>0.09 ± 0.02</td>
<td>0.05 ± 0.04</td>
</tr>
<tr>
<td>0.2</td>
<td>0.54 ± 0.06</td>
<td>0.41 ± 0.03</td>
<td>0.14 ± 0.04</td>
<td>0.09 ± 0.02</td>
<td>0.08 ± 0.04</td>
</tr>
<tr>
<td>0.3</td>
<td>0.48 ± 0.06</td>
<td>0.40 ± 0.03</td>
<td>0.09 ± 0.04</td>
<td>0.10 ± 0.02</td>
<td>0.12 ± 0.05</td>
</tr>
<tr>
<td>0.5</td>
<td>0.37 ± 0.06</td>
<td>0.41 ± 0.03</td>
<td>0.05 ± 0.04</td>
<td>0.11 ± 0.02</td>
<td>0.22 ± 0.06</td>
</tr>
</tbody>
</table>

Fluxes are expressed in $\mu$mol·g$^{-1}$·min$^{-1}$ and shown as means ± SE. $^{*}$Glu$^{\alpha} = \alpha$Glu$^{tot}$, Glu$^{\alpha} = (1 - \alpha)$Glu$^{tot}$, where Glu$^{tot}$ = Glu$^{\alpha} +$ Glu$^{\alpha}$.

### Table 6. Sensitivity of $V_{PDH}$, $V_{NT}$, $CMR_{Glc(oxy)}$, $V_G$, and $V_{PC}$ to the assumed cellular distribution of glutamine

<table>
<thead>
<tr>
<th>$\beta^*$</th>
<th>$V_{PDH}$</th>
<th>$CMR_{Glc(oxy)}$</th>
<th>$V_{NT}$</th>
<th>$V_{PC}$</th>
<th>$V_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.033</td>
<td>0.61 ± 0.07</td>
<td>0.43 ± 0.04</td>
<td>0.25 ± 0.07</td>
<td>0.09 ± 0.02</td>
<td>0.05 ± 0.05</td>
</tr>
<tr>
<td>0.25</td>
<td>0.62 ± 0.07</td>
<td>0.43 ± 0.04</td>
<td>0.25 ± 0.07</td>
<td>0.09 ± 0.02</td>
<td>0.04 ± 0.05</td>
</tr>
<tr>
<td>0.5</td>
<td>0.63 ± 0.07</td>
<td>0.44 ± 0.05</td>
<td>0.25 ± 0.07</td>
<td>0.10 ± 0.02</td>
<td>0.05 ± 0.05</td>
</tr>
</tbody>
</table>

Values are means ± SE expressed in $\mu$mol·g$^{-1}$·min$^{-1}$. $^{*}$Gln$^{\alpha} = \beta$Gln$^{tot}$, Gln$^{\alpha} = Gln^{\alpha}$.
maximum afforded by $V_{PDH}$. A low rate of exchange between OG and Glu on the order of the flux through pyruvate dehydrogenase implies that the malate-aspartate shuttle is a substantial mechanism by which label is exchanged between the cytosolic amino acids Glu and Asp and their metabolic partners in the TCA cycle. This points to the potential that the rate of exchange between Glu and OG can change under widely varying metabolic conditions and thus cannot a priori be assumed to be at a constant high level.

Recently, it has been postulated that the rate of glutamatergic action, assumed to correspond to the rate of neuronal Glu uptake into glia and interconversion to Gln (also termed the glutamate-glutamine “cycle”) is stoichiometrically related to the oxidative glucose consumption, $\text{CMR}_{\text{Glc(ox)}}$. In our study, this ratio was found to be substantially lower than the 1:1 ratio reported in rat brain (57, 67). The differences can potentially be ascribed to two assumptions in that study, namely that turnover of Glu C4 was assumed to represent total $\text{CMR}_{\text{Glc(ox)}}$, and turnover of Gln C4 was assumed to represent exclusively the glutamate-glutamine “cycle.” Indeed, in our study we find that when the flux through glutamine synthetase, $V_{\text{syn}}$, was correlated with the oxidative glucose consumption, $\text{CMR}_{\text{Glc(ox)}}$, a ratio of 0.8 ± 0.2 was calculated that is much closer to the reported relative rates. However, the contribution of pyruvate carboxylation needs to be subtracted from the flux through glutamine synthetase, resulting in a substantial reduction of this ratio. In this calculation, it should be noted that nonoxidative contributions to the overall flux through hexokinase, glycogen metabolism (13), as well as metabolism of GABAergic neurons, have not been taken into account, which would lead to an even larger discrepancy between the ATP produced by the glial compartment and the ATP required for the Glu-Gln cycle. Furthermore, it has been shown that astrocytes can increase their oxygen consumption after glutamate uptake (18). Nevertheless, it is quite possible that some form of monotonic relationship exists between energy metabolism and glutamatergic action, yet the precise relationship still remains to be fully characterized.

The presented results can depend on the assumed distribution of glutamate between the glial and neuronal compartments. For example, the assumed intercellular distribution of glutamate has a strong effect on the calculated rates (Table 5). The parameter that was systematically varied was $\alpha$, which was defined through the following relationships: $\text{Glu}^{(g)} = \alpha \text{Glu}_{\text{tot}}$, $\text{Glu}^{(n)} = (1 - \alpha \text{Glu}_{\text{tot}})$, where $\text{Glu}_{\text{tot}} = \text{Glu}^{(g)} + \text{Glu}^{(n)}$. Likewise, the effect of changing the cellular distribution of glutamine was shown by varying the parameter $\beta$, defined by the relationships $\text{Gln}^{(n)} = \beta \text{Gln}_{\text{tot}}$, $\text{Gln}^{(g)} = (1 - \beta \text{Gln}_{\text{tot}})$, where $\text{Gln}_{\text{tot}} = \text{Gln}^{(g)} + \text{Gln}^{(n)}$, which was without effect on the modeling (Table 6). However, even the assumption that all but 3.3% of the metabolic glutamate pool is in neurons does not affect our suggestion that the relationship between glutamatergic action and glucose consumption is not stoichiometric, because this relationship increased only to ~0.6, oxidative generation of ATP in astrocytes decreased to ~82%, and glial relative to neuronal ATP generation was reduced to ~10%. Interestingly, in all simulations, the total oxidative glucose consumption remains a very stable measurement. The proposed modeling is subject to further refinement, but we think we have attempted the most complete modeling with the least number of assumptions to date. Our study, therefore, underlines the importance of making such assumptions in modeling complex biological data, and the recognition that previous models based on simpler data need to be considered with appropriate caution.

We conclude that pyruvate carboxylation may be a significant contributor to the flux through glutamine synthetase in the human brain in vivo. Glutamatergic action contributes to the flux through glutamine synthetase, but we conclude that, at rest, oxidative glucose consumption is not necessarily 1:1 stoichiometrically correlated with glutamatergic action. Finally, we conclude that the exchange of label between 2-oxoglutarate and glutamate may be affected by the cellular energy status.

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